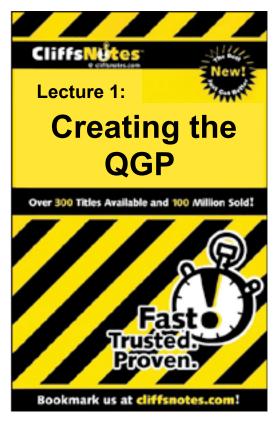
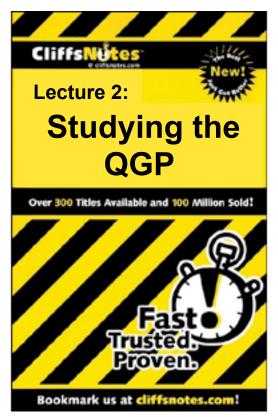
Studying a new Phase of Matter An introduction to the Quark Gluon Plasma and Relativistic Heavy Ion Physics





2010 Hadron Collider Physics Summer School

Fermi Lab - August 2010

Helen Caines - Yale University

Relativistic Heavy Ions I The What, Where, Why, and How of It All

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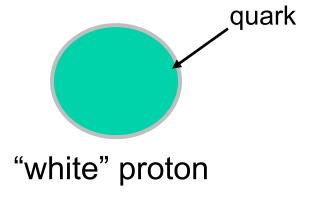
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Outline:

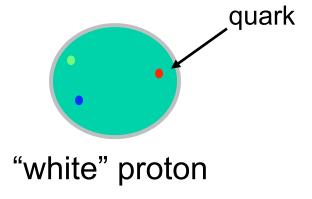
QCD and Asymptotic Freedom
The Quark Gluon Plasma
The Accelerators & Experiments
Evidence for the QGP



Confinement: fundamental & crucial feature of strong interaction force = const has significant consequences



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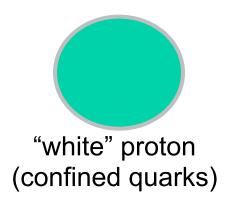
Confinement: fundamental & crucial feature of strong interaction force = const has significant consequences

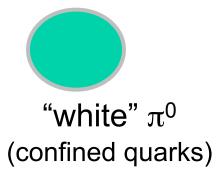
Strong color field
Force grows with
separation !!!

Confinement: fundamental & crucial feature of strong interaction force = const has significant consequences

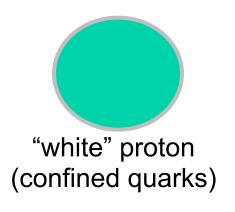
quark-antiquark pair created from vacuum

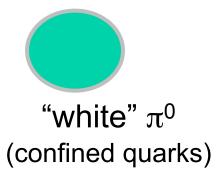
Confinement: fundamental & crucial feature of strong interaction force = const has significant consequences





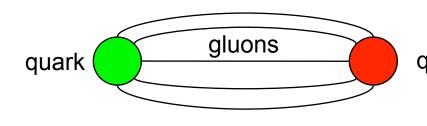
Confinement: fundamental & crucial feature of strong interaction force = const has significant consequences





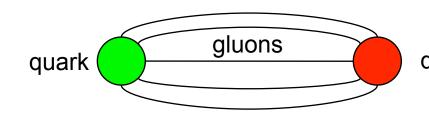
To understand the strong force and confinement: Create and study a system of deconfined colored quarks and gluons

We don't see free quarks



Strong force becomes a quark constant at ~size of a hadron which is ~1 fm (10⁻¹⁵ m)

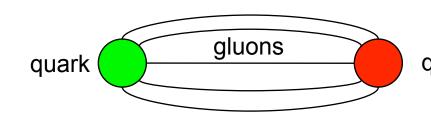
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$$1\frac{GeV}{fm} = \frac{10^9 eV}{10^{-15}m} \times \frac{1.6 \times 10^{-19}J}{eV} = 1.6 \times 10^5 N$$

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Compare to gravitational force at Earth's surface

$$F = 1.6 \times 10^5 N = M \times g = M \times 9.8 m/s^2$$

$$M = 16,300kg$$

Quarks exert 16 metric tons of force on each other!

Coupling constant is not a "constant"

Runs with Q² (mtm transfer) accounts for vacuum polarisation

$$\alpha_s(Q^2) = \frac{\alpha_s(\mu^2)}{\left[1 + (\alpha_s(\mu^2)\frac{(33 - 2n_f)}{12\pi})ln(Q^2/\mu^2)\right]}$$

 $\alpha_{\rm s}(\mu^2) \sim 1 !!$

μ²: renormalization scale

33: gluon contribution

nf: # quark flavours

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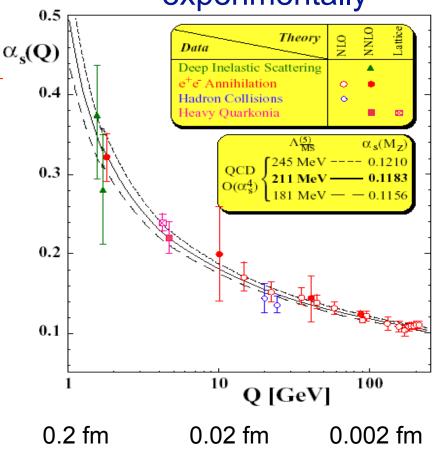
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Running measured experimentally



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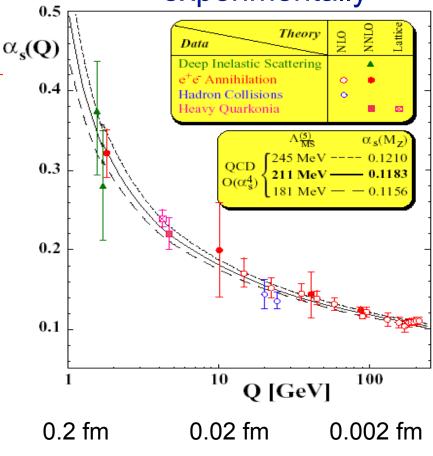
$$\alpha_s(Q^2) \to 0$$
, as $Q \to \infty$, $r \to 0$

Coupling very weak

→ partons are essentially free

Asymptotic Freedom

Running measured experimentally



Coupling constant is not a "constant"

Runs accou



The Nobel Prize in Physics 2004

ured lly

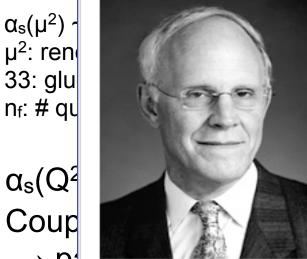
0.1183

-0.1156

 $\alpha_s(Q^2)$

"for the discovery of asymptotic freedom in the theory of the strong interaction"

 $\alpha_s(\mu^2)$ μ²: ren 33: glu



David J. Gross



H. David Politzer



Frank Wilczek

Asymptotic Freedom

0.2 fm

 $0.02 \, \text{fm}$

 $\overline{0}$.002 fm

100

Asymptotic freedom vs Debye screening

Asymptotic freedom occurs at very high Q² Problem: Q² much higher than available in the lab.

So how to create and study this new phase of matter? Solution: Use effects of Debye screening

In the presence of many colour charges (charge density n), the short range term of the strong potential is modified:

Charges at long range (r > r_D) are screened

Asymptotic freedom vs Debye screening

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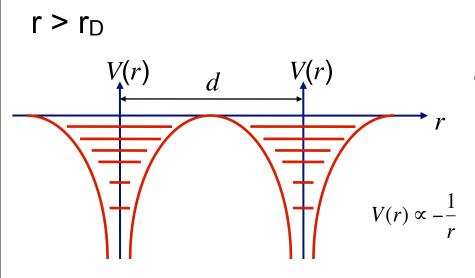
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$$V_s(r) \propto rac{1}{r} \Longrightarrow rac{1}{r} exp[rac{-r}{r_D}]$$
 where $r_D = rac{1}{3\sqrt{n}}$ is the Debye radius

Charges at long range (r > r_D) are screened

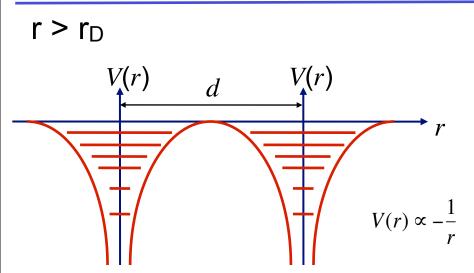
QED and Debye screening



In condensed matter this leads to an interesting transition

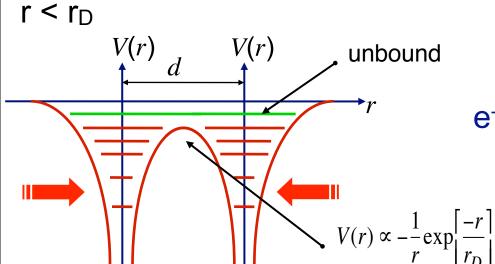
e⁻ separation > e⁻ binding radius → insulator

QED and Debye screening



In condensed matter this leads to an interesting transition

e⁻ separation > e⁻ binding radius → insulator



e⁻ separation < e⁻ binding radius → conductor

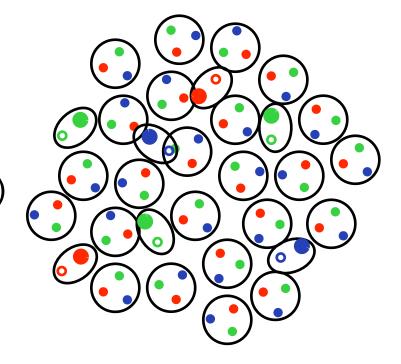
This is the Mott Transition

QCD and Debye screening

At low colour densities:

quarks and gluons confined into colour singlets

→ hadrons (baryons and mesons)

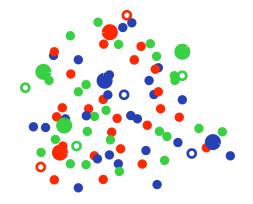


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At high colour densities:

quarks and gluons unbound Debye screening of colour charge

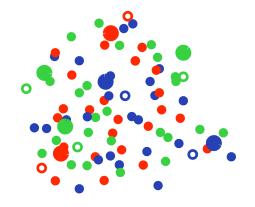
→ QGP - colour conductor

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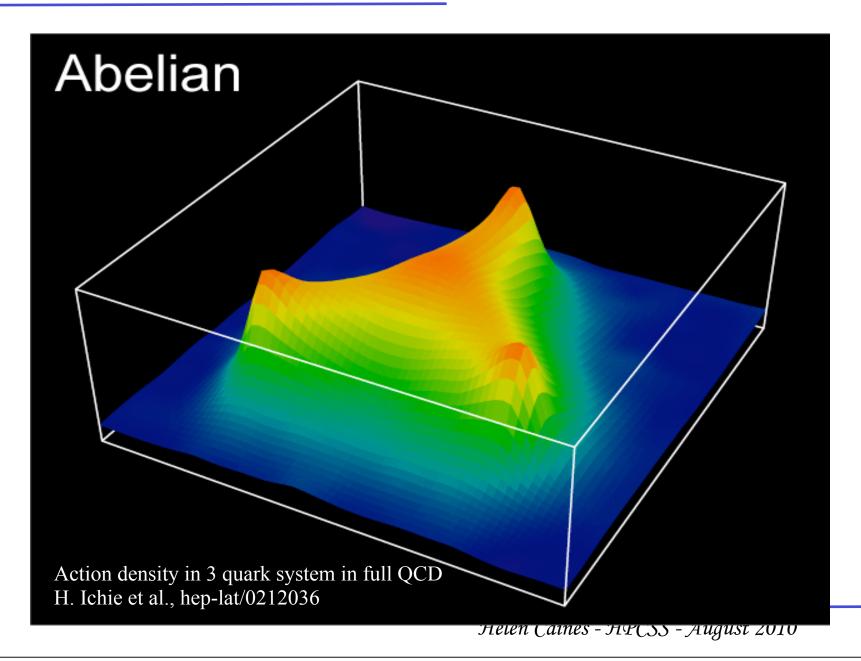
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→ QGP - colour conductor

Can create high colour density by heating or compressing

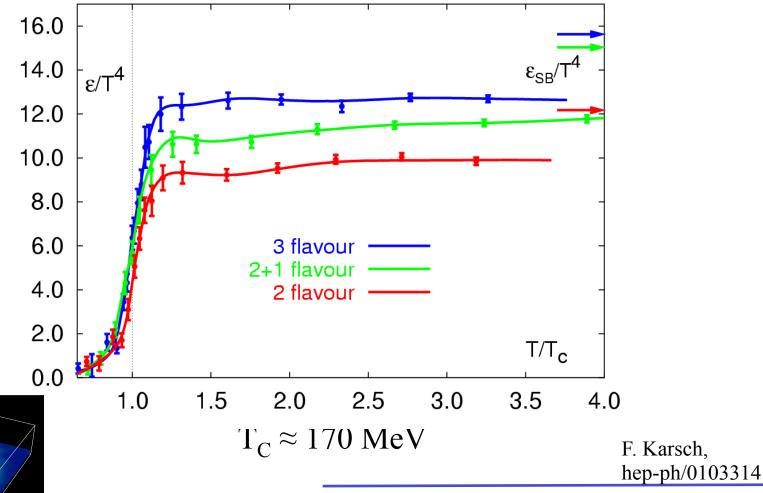
→ QGP creation via accelerators or in neutron stars

What is T_c ? - Lattice QCD



What is T_c ? - Lattice QCD

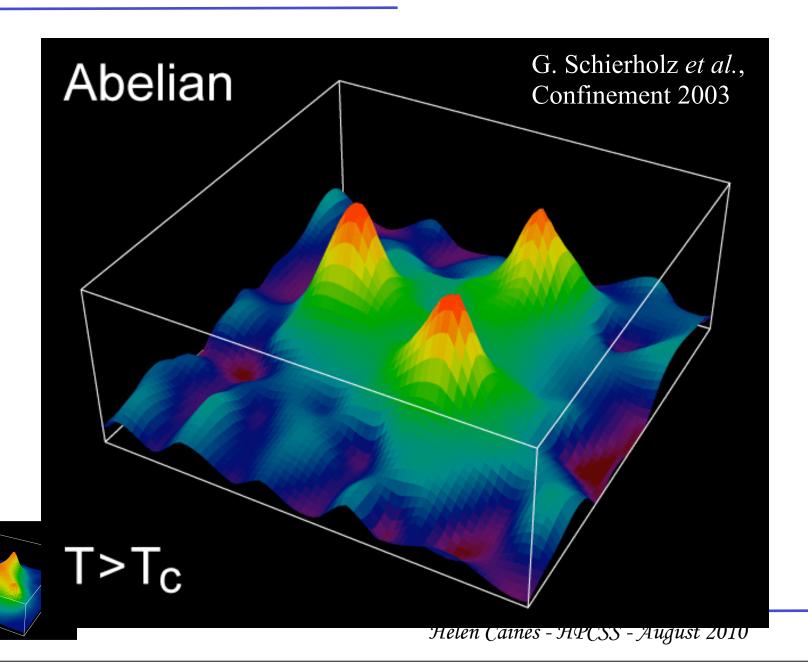
- Coincident transitions: deconfinement and chiral symmetry restoration
- Recently extended to $\mu_B > 0$, order still unclear (1st, 2nd, crossover?)



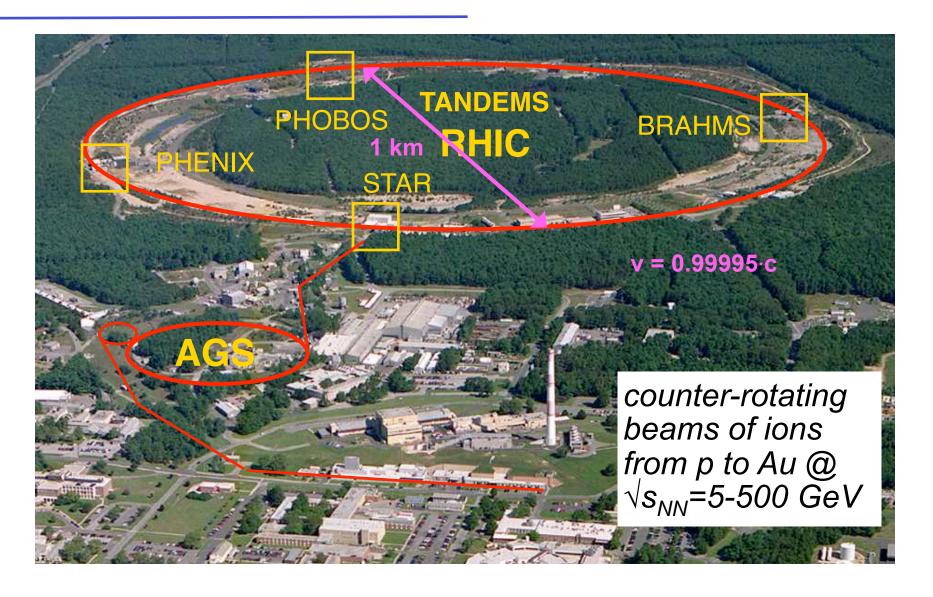
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Abelian

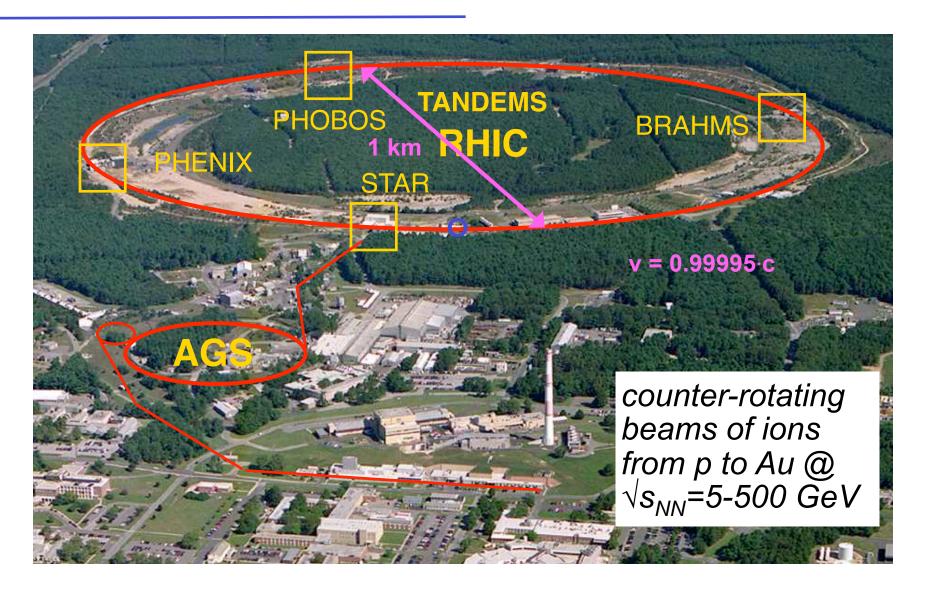
What is T_c ? - Lattice QCD



RHIC - a collider



RHIC - a collider

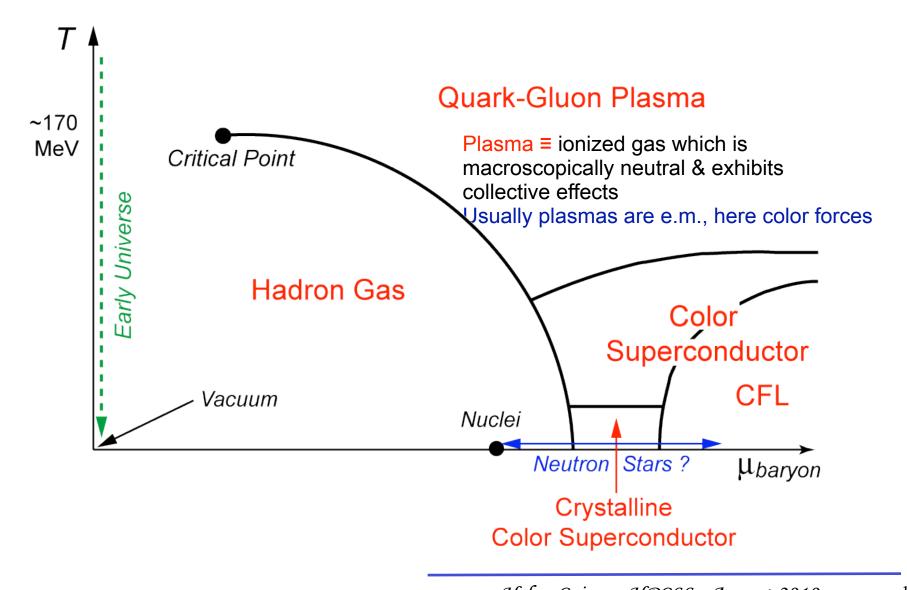


RHIC and the LHC

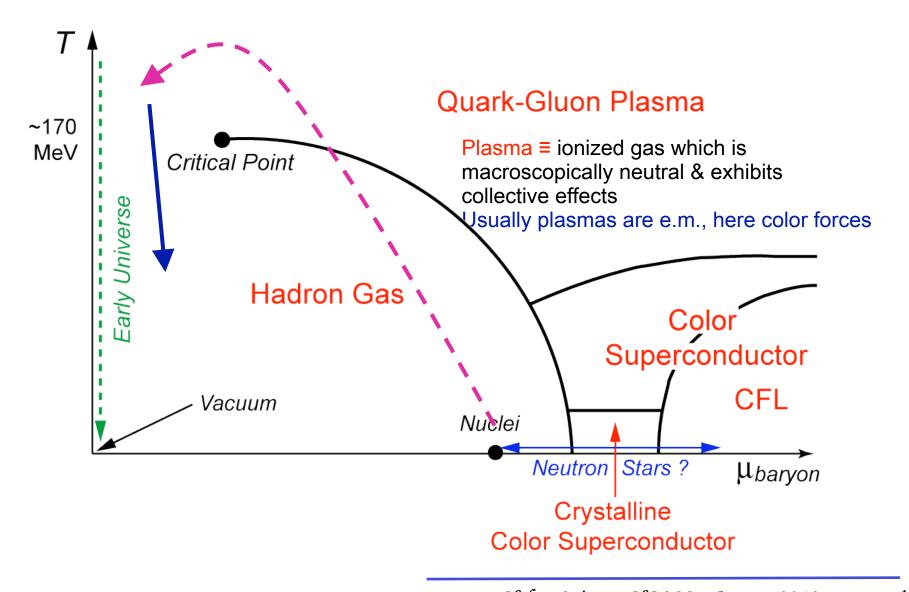
	RHIC	LHC
Start date	2001	2009
Ion	Au-Au & p-p	Pb-Pb & p-p
Max √s	200 GeV	5.5 TeV
Circumference	2.4 miles	17 miles
Depth	On surface	175 m below ground
HI Exp.	BRAHMS, PHENIX, PHOBOS, STAR	ALICE, ATLAS, CMS
Located	BNL, New York, USA	CERN, Geneva, Switzerland

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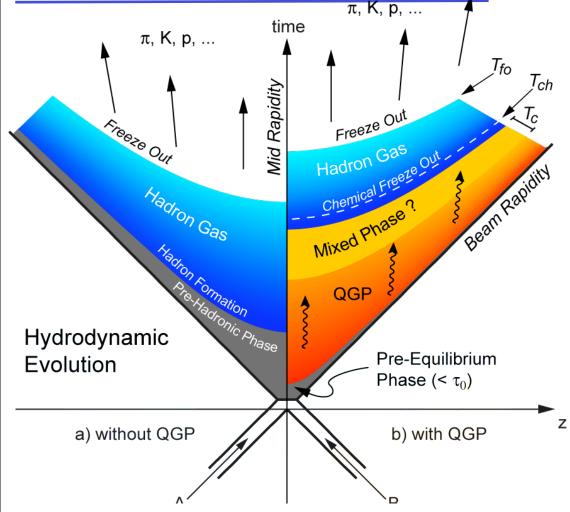
QCD phase diagram of hadronic matter



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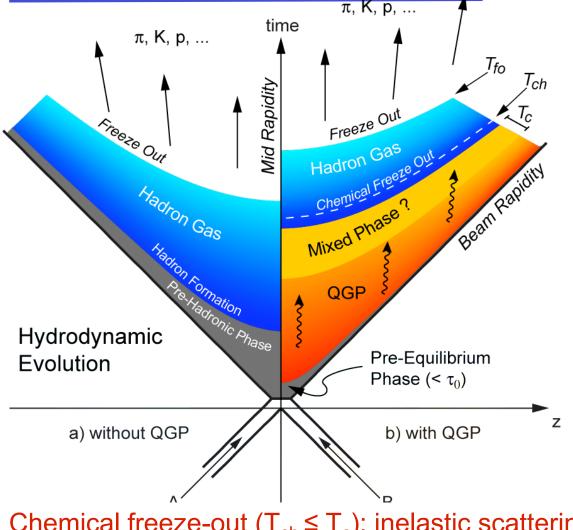
The phase transition in the laboratory



Chemical freeze-out (T_{ch} ≤ T_c): inelastic scattering ceases

Kinetic freeze-out ($T_{fo} \le T_{ch}$): elastic scattering ceases

The phase transition in the laboratory



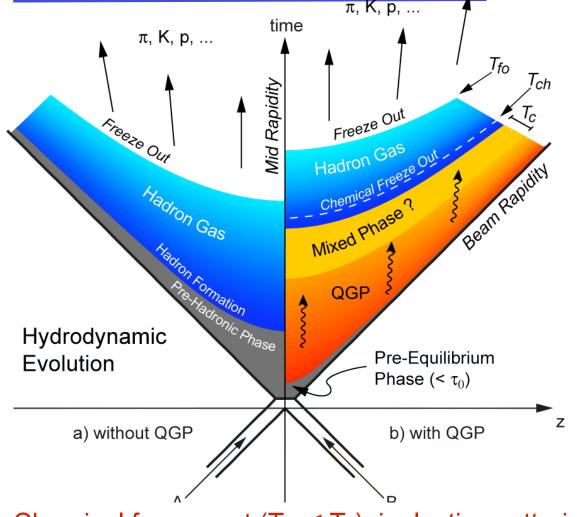
Lattice (2-flavor): $T_C \approx 173\pm 8 \text{ MeV}$ $\varepsilon_C \approx (6\pm 2) T^4 \approx 0.70 \text{ GeV/fm}^3$

Remember: cold nuclear matter $\varepsilon_{cold} \approx u / {}^{4}/_{3} \pi r_{0}{}^{3} \approx 0.13 \text{ GeV/fm}^{3}$

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Necessary but **not** sufficient condition

Tevatron (Fermilab) $\varepsilon(\sqrt{s} = 1.8 \text{TeV pp}) >> \varepsilon(\sqrt{s} = 200 \text{GeV Au+Au RHIC})$

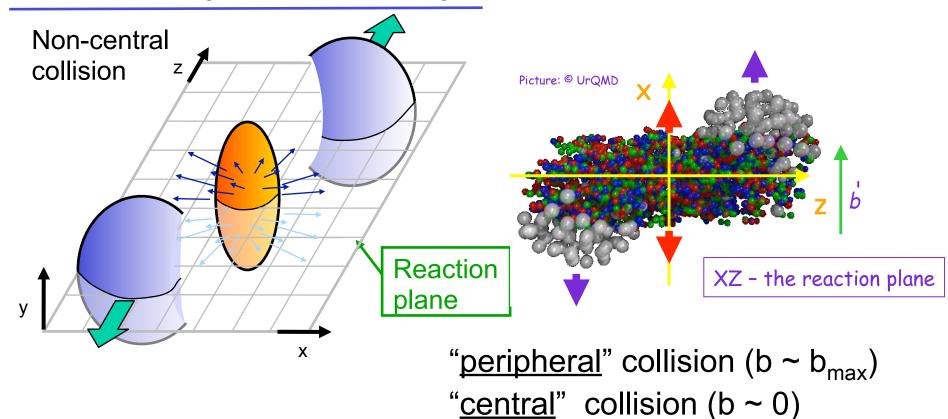
Thermal Equilibrium ⇒ many constitutents

Chemical freeze-out $(T_{ch} \le T_c)$: inelastic scattering ceases

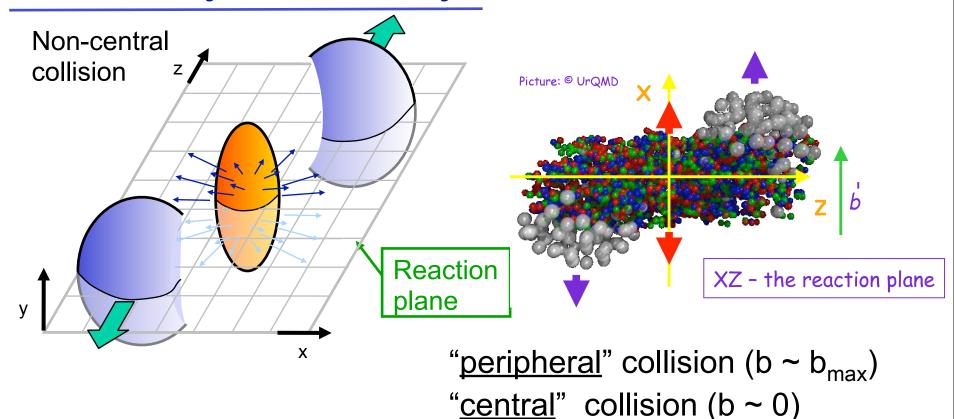
Size matters !!!

Kinetic freeze-out ($T_{fo} \le T_{ch}$): elastic scattering ceases

Geometry of a heavy-ion collision



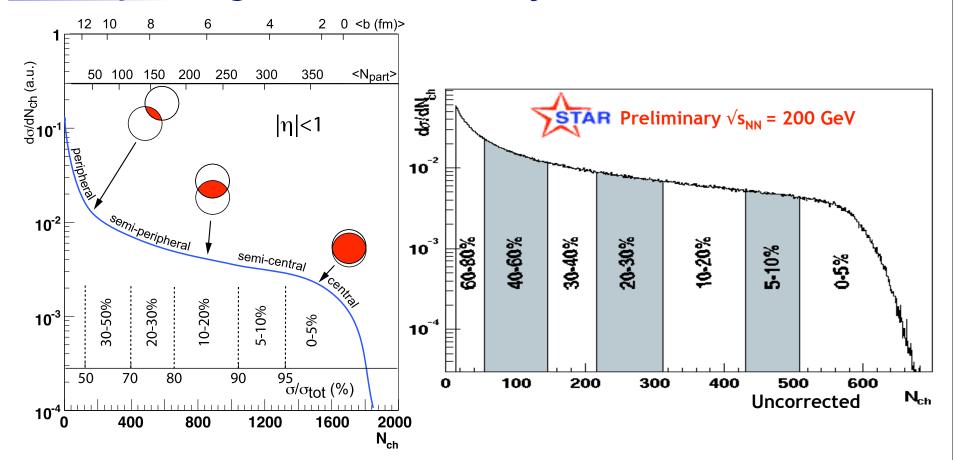
Geometry of a heavy-ion collision



Number of participants (N_{part}): number of incoming nucleons (participants) in the overlap region Number of binary collisions (N_{bin}): number of equivalent inelastic nucleon-nucleon collisions $N_{bin} \ge N_{part}/2$

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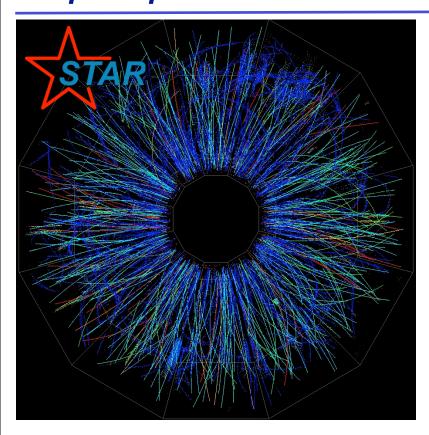
Comparing to data heavy-ion collision



Good agreement between data and calculation

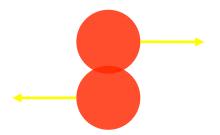
Measured mid-rapidity particle yield can be related to size of overlap region

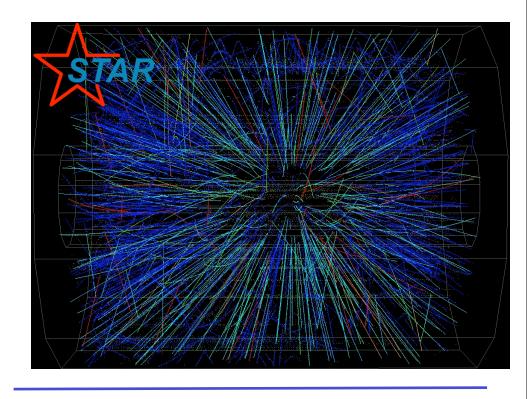
A peripheral Au-Au collision



Color ⇒ Energy loss in TPC gas

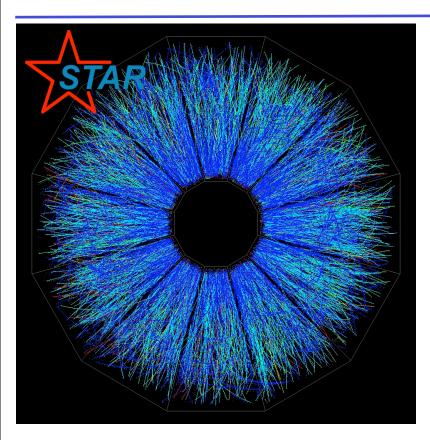
Peripheral Collision





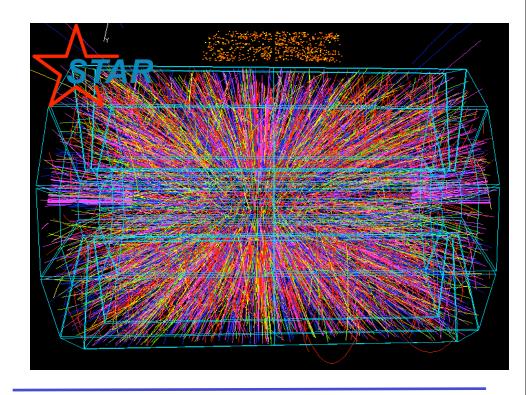
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39.4 TeV in central Au-Au collision

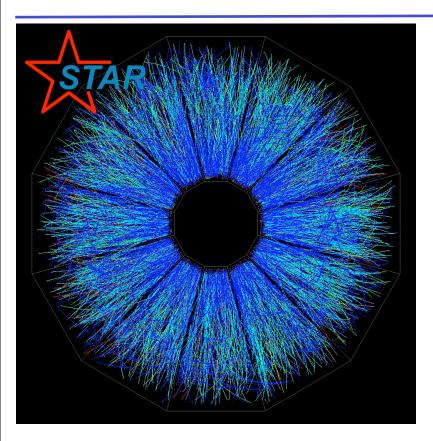


>5000 hadrons and leptons

- Only charged particles shown
- Neutrals don't ionise the TPC's gas so are not "seen" by this detector.



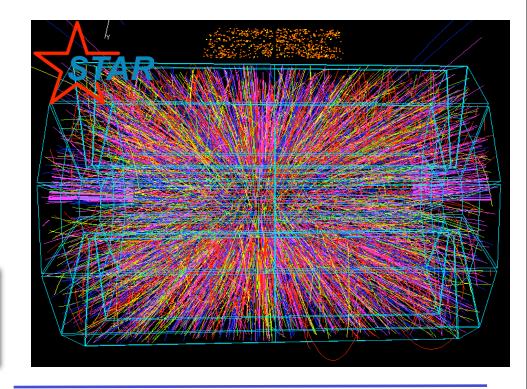
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26 TeV is removed from colliding beams.

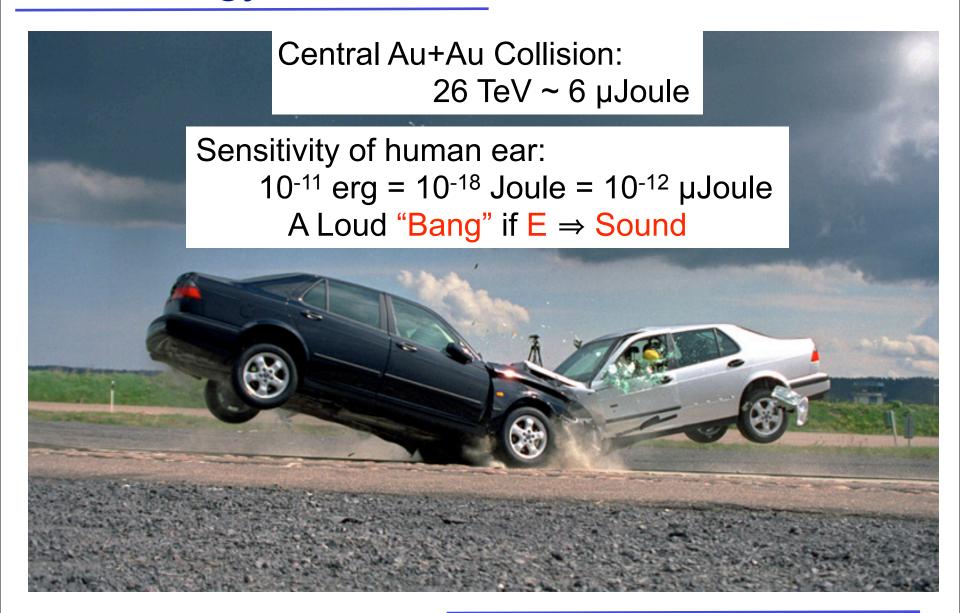
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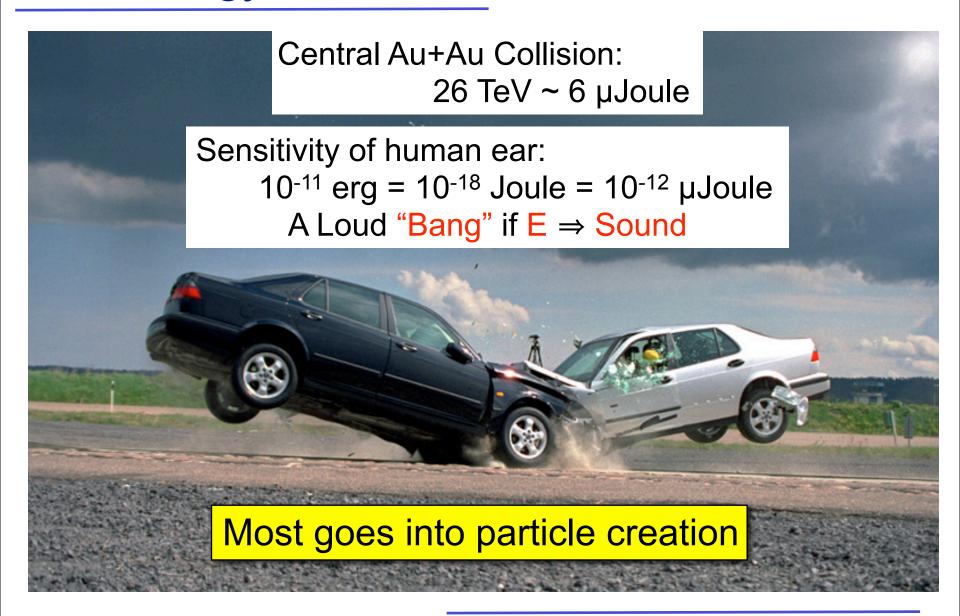
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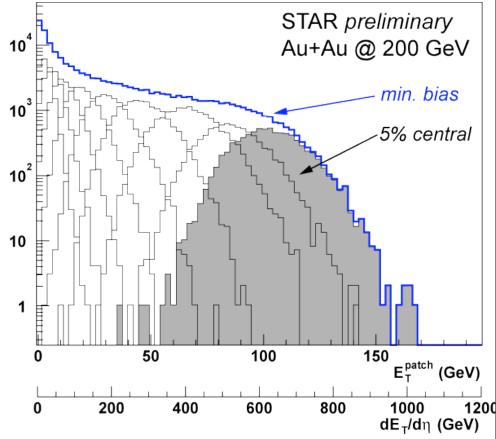


The energy is contained in one collision



Energy density in central Au-Au collisions

 use calorimeters to measure total energy



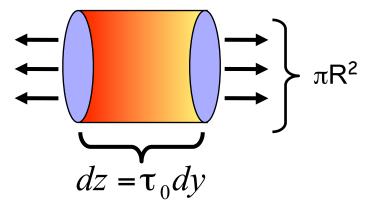


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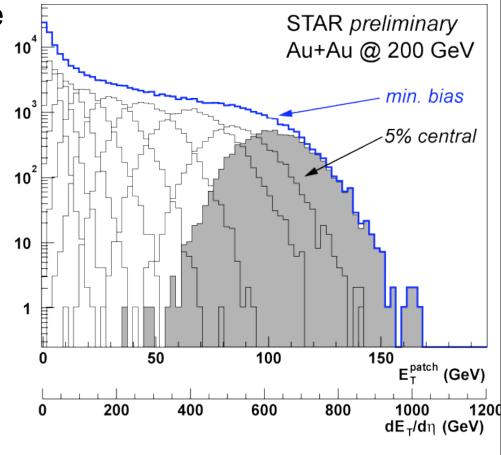
- use calorimeters to measure total energy
- estimate volume of collision

Bjorken-Formula for Energy Density:

$$\varepsilon_{Bj} = \frac{\Delta E_T}{\Delta V} = \frac{1}{\pi R^2} \frac{1}{\tau_0} \frac{dE_T}{dy}$$
Time it takes to thermalize system



 $(t_0 \sim 1 \text{ fm/c})$



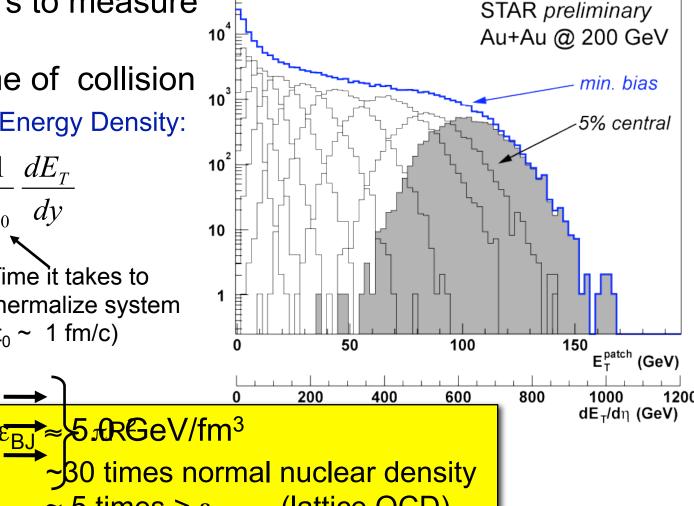
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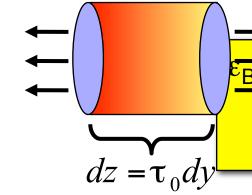
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Time it to the results

Time it takes to thermalize system $(t_0 \sim 1 \text{ fm/c})$





~30 times normal nuclear density

~ 5 times > $\varepsilon_{\text{critical}}$ (lattice QCD)

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5 GeV/fm³. Is that a lot?

In a year, the U.S. uses ~100 quadrillion BTUs of energy (1 BTU = 1 burnt match):

$$100 \times 10^{15} BTU \times \frac{1060J}{BTU} \times \frac{1eV}{1.6 \times 10^{-19}J} = 6.6 \times 10^{38} eV$$

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At 5 GeV/fm³, this would fit in a volume of:

$$6.6 \times 10^{38} eV \div \frac{5 \times 10^9 eV}{fm^3} = 1.3 \times 10^{29} fm^3$$

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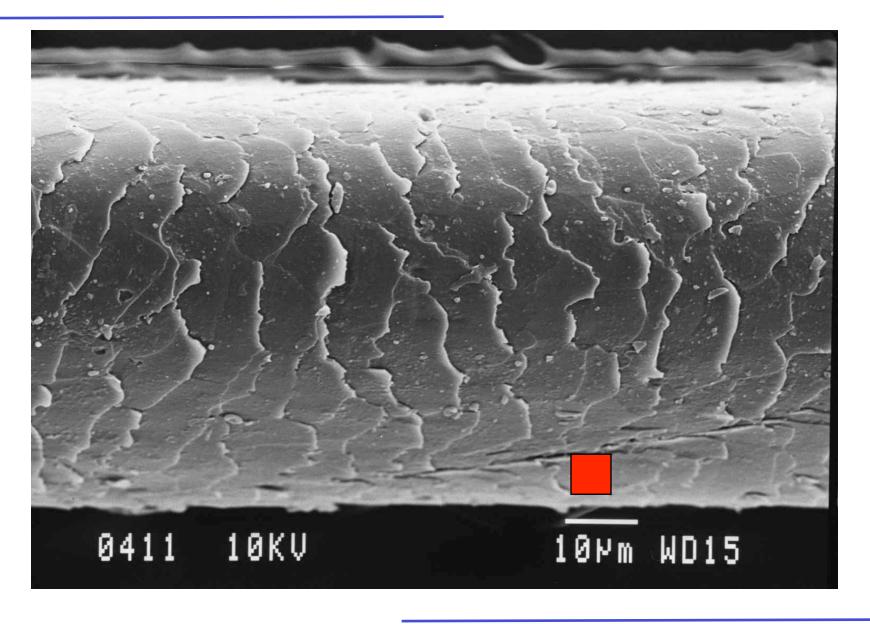
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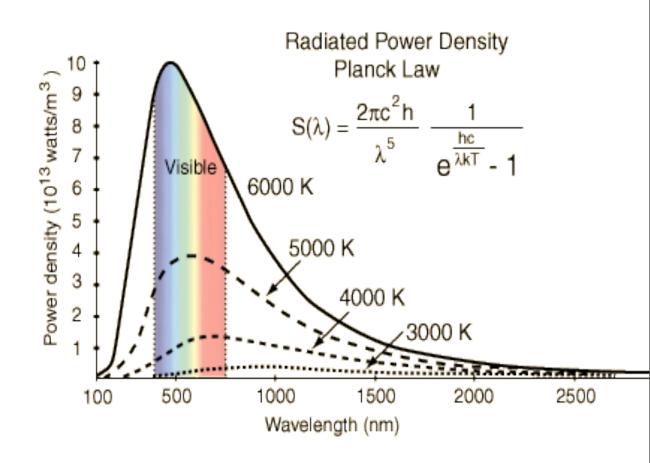
Or, in other words, in a box of the following dimensions:

$$\sqrt[3]{1.3 \times 10^{29} \, fm^3} = 5 \times 10^9 \, fm = 5 \, \mu m$$

A human hair



Planck distribution describes intensity as a function of the wavelength of the emitted radiation



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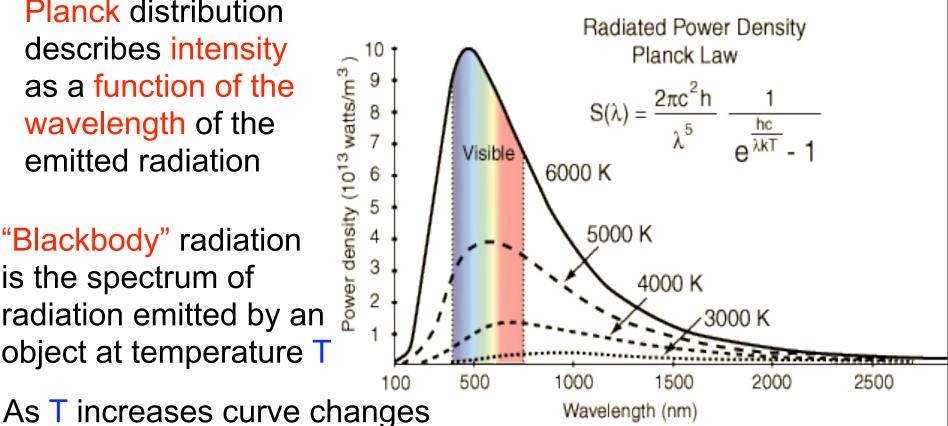
"Blackbody" radiation is the spectrum of radiation emitted by an object at temperature T

Radiated Power Density Planck Law Power density (10¹³ watts/m³ Visible 6000 K 5000 K 4000 K 3000 K 1000 2000 500 1500 2500 100 As T increases curve changes Wavelength (nm)

Photons have no charge or color → don't interact with medium

Planck distribution describes intensity as a function of the wavelength of the emitted radiation

"Blackbody" radiation is the spectrum of radiation emitted by an object at temperature T

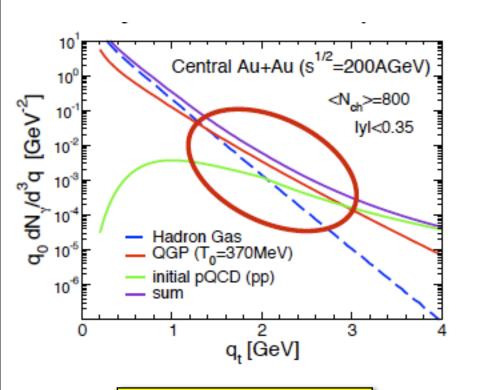


Photons have no charge or color → don't interact with medium

γ reveals early temperature of QGP

γ emitted over all lifetime → convolution of all temperatures

Theory now well developed



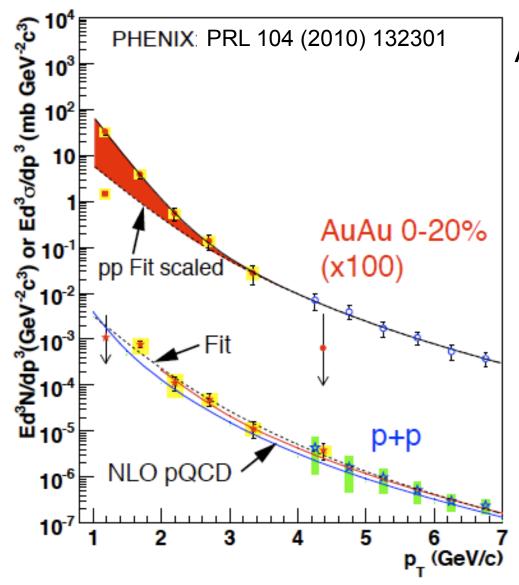
QGP dominates 1< p_T< 3 GeV/c

Corrections under control

Experimentally photons a complete pain!

Calorimetry
granularity and resolution
Large background
π⁰/η→γγ
Losses from conversions
Hadronic contamination

Signal:Background ~1:10



After background subtraction:

Emission rate and shape consistent with that from a hot thermally equilibrated medium

$$T = 300 - 600 \text{ MeV}$$

 $\tau = 0.15-0.6 \text{ fm/c}$

Large uncertainty due to correlated pair background i.e. jets

What is the temperature of the medium?

- Statistical Thermal Models:
 - Assume a system that is thermally (constant T_{ch}) and chemically (constant n_i) equilibrated
 - System composed of non-interacting hadrons and resonances
 - Obey conservation laws: Baryon Number, Strangeness, Isospin
- Given T_{ch} and μ 's (+ system size), n_i's can be calculated in a grand canonical ensemble

$$n_i = \frac{g}{2\pi^2} \int_0^\infty \frac{p^2 dp}{e^{(E_i(p) - \mu_i)/T} \pm 1}, E_i = \sqrt{p^2 + m_i^2}$$

Fitting the particle ratios

Number of particles of a given species related to temperature

$$dn_i \sim e^{-(E-\mu_B)/T} d^3 p$$

- Assume all particles described by same temperature T and μ_B
- one ratio (e.g., p / p)
 determines μ / T :

$$\frac{\bar{p}}{p} = \frac{e^{-(E + \mu_B)/T}}{e^{-(E - \mu_B)/T}} = e^{-2\mu_B/T}$$

• A second ratio (e.g., K / π) provides T $\rightarrow \mu$

$$\frac{K}{\pi} = \frac{e^{-E_K/T}}{e^{-E_\pi/T}} = e^{-(E_K - E_\pi)/T}$$

 Then all other hadronic ratios (and yields) defined

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Number of particles of a given species related to temperature

$$dn_i \sim e^{-(E-\mu_B)/T} d^3 p$$

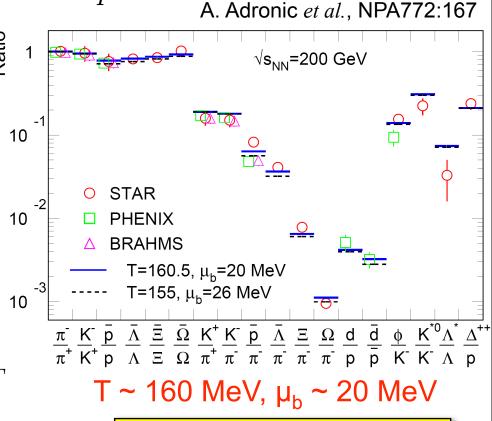
- Assume all particles described by same temperature T and µB
- one ratio (e.g., p / p)
 determines μ / T :

$$\frac{\bar{p}}{p} = \frac{e^{-(E + \mu_B)/T}}{e^{-(E - \mu_B)/T}} = e^{-2\mu_B/T}$$
 10 -2

• A second ratio (e.g., K / π) provides T $\rightarrow \mu$

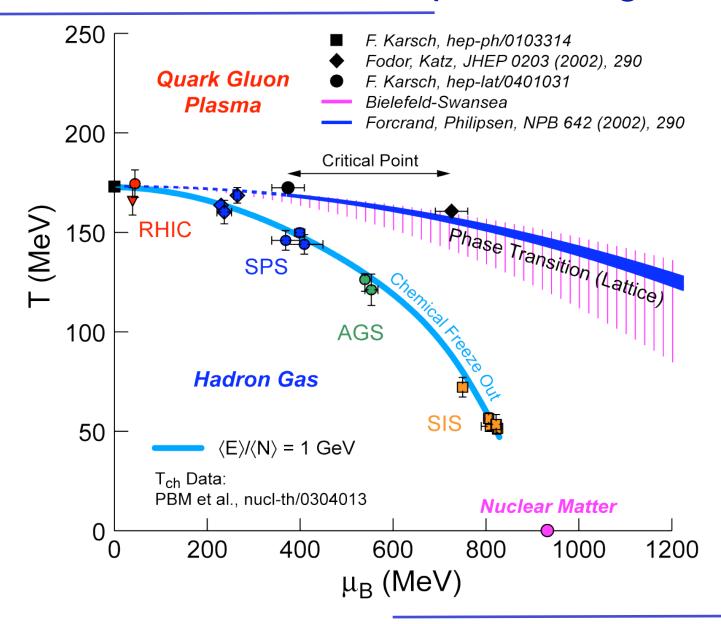
$$\frac{K}{\pi} = \frac{e^{-E_K/T}}{e^{-E_\pi/T}} = e^{-(E_K - E_\pi)/T}$$

 Then all other hadronic ratios (and yields) defined

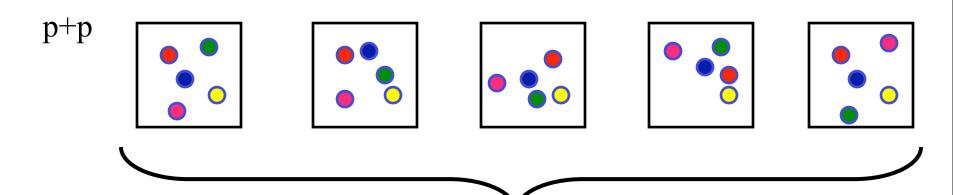


Initial Temperature probably much higher

Where RHIC sits on the phase diagram

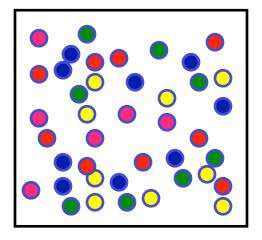


Statistics ≠ thermodynamics



Ensemble of events constitutes a statistical ensemble T and μ are simply Lagrange multipliers "Phase Space Dominance"

A+A



One (1) system is already statistical!

- We can talk about pressure
- T and μ are more than Lagrange multipliers

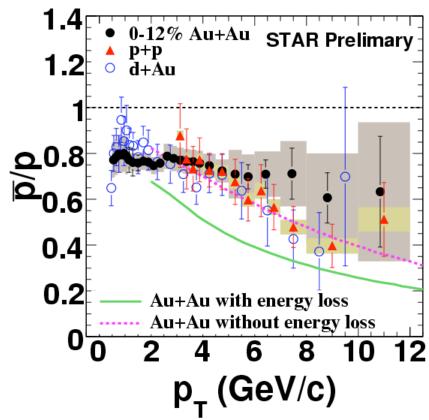
By the way!

Take a second look at the anti-proton/proton ratio

 $\frac{-}{p}/p \sim 0.8$

There is a net baryon number at mid-rapidity!!

Baryons number is being transported over 6 units of rapidity from the incoming beams to the collision zone!



Baryon number not carried by quarks

- baryon junctions postulated

Evidence for thermalization?

- Not all processes which lead to multi-particle production are thermal - elementary collisions
- Any mechanism for producing hadrons which evenly populates the free particle phase space will mimic a microcanonical ensemble.
- Relative probability to find n particles is the ratio of the phase-space volumes $P_n/P_{n'} = \varphi_n(E)/\varphi_{n'}(E) \Rightarrow$ given by statistics only.
- Difference between MCE and CE vanishes as the size of the system N increases.
- Such a system is NOT in thermal equilibrium to thermalize need interactions/re-scattering

Need to look for other evidence of collective motion

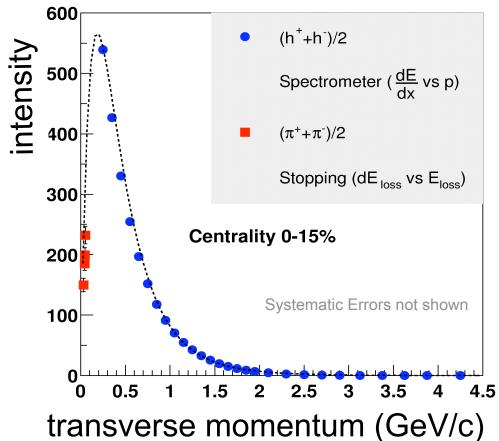
Determining the temperature

1/Wavelength ~ Freq ~ E ~ p

From transverse momentum distribution of pions deduce temperature ~120 MeV

$$E = \frac{3}{2}kT$$

$$T = \frac{2E}{3k}$$



$$= \frac{2 \times 120 \times 10^6}{3 \times 1.4 \times 10^{-23}} \times 1.6 \times 10^{-19}$$

$$\sim 9 \times 10^{11} K$$

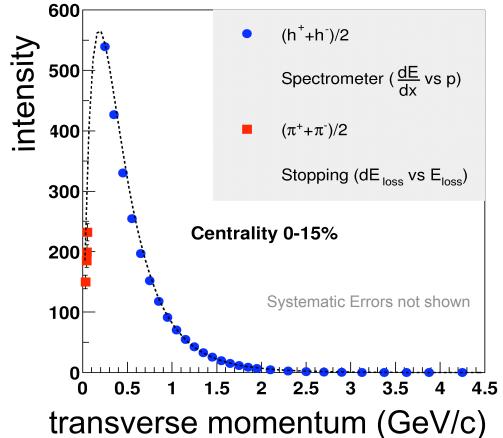
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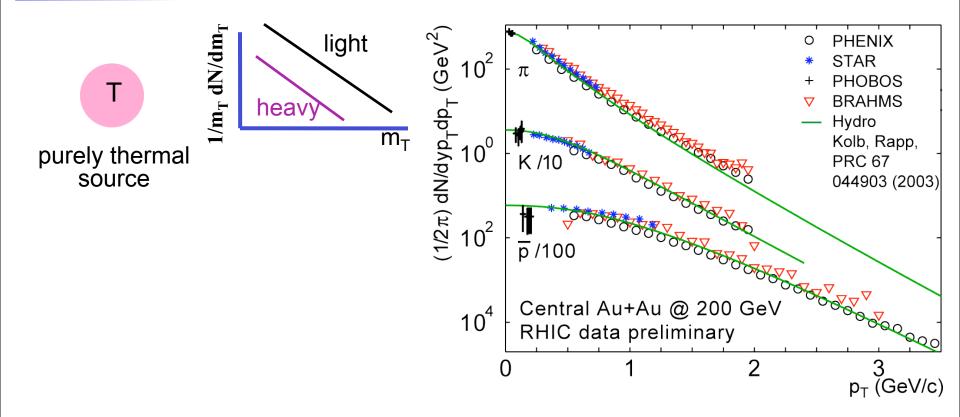


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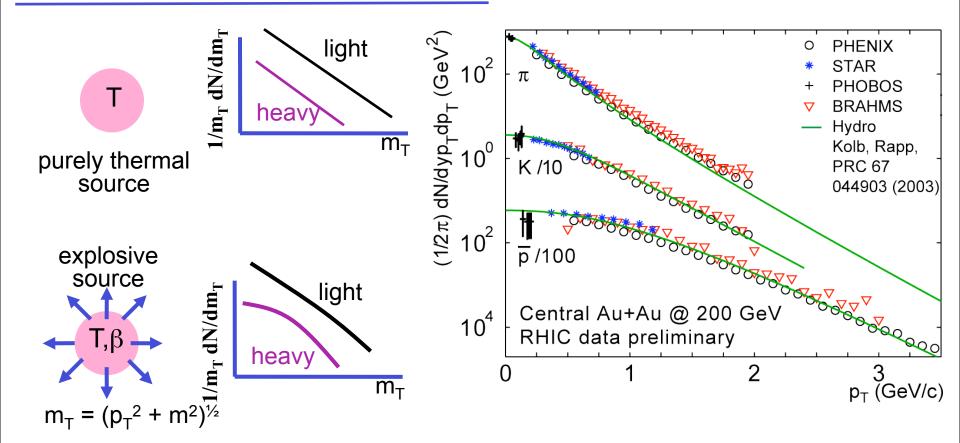
 $\sim 9 \times 10^{11} K$

System exist for time in hadronic phase

Strong collective radial expansion

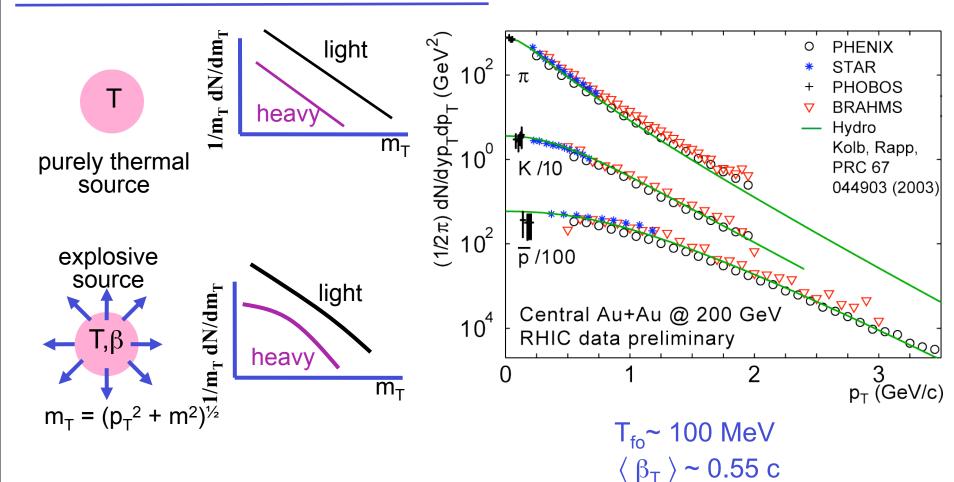


Strong collective radial expansion



- Different spectral shapes for particles of differing mass
 - → strong collective radial flow

Strong collective radial expansion



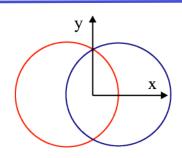
- Different spectral shapes for particles of differing mass
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Good agreement with hydrodynamic prediction for soft EOS (QGP+HG)

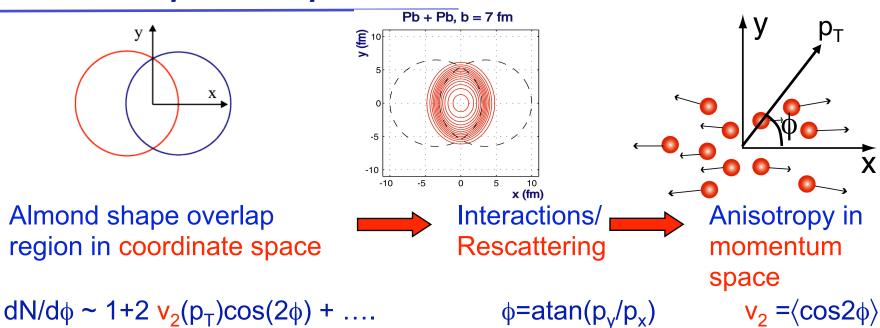
32

p_T (GeV/c)

Anisotropic/Elliptic flow

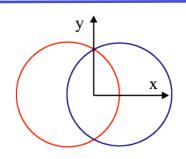


Almond shape overlap region in coordinate space



$$v_2$$
: 2nd harmonic Fourier coefficient in dN/d ϕ with respect to the reaction plane

Anisotropic/Elliptic flow



Almond shape overlap region in coordinate space Pb + Pb, b = 7 fm

Interactions/ Rescattering

Anisotropy in

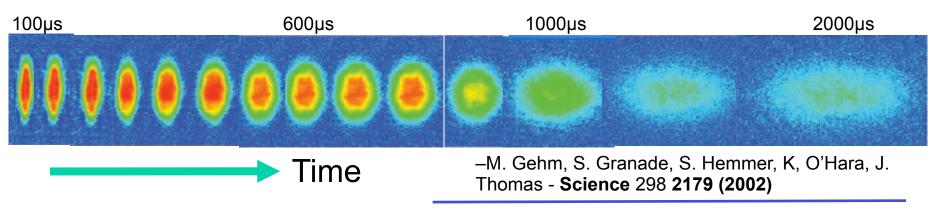
momentum space

$$v_2 = \langle \cos 2\phi \rangle$$

$$dN/d\phi \sim 1+2 v_2(p_T)\cos(2\phi) + \dots$$

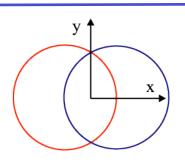
$$\phi$$
=atan(p_y/p_x)

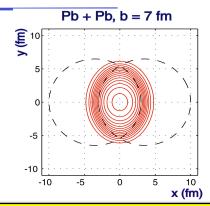
 V_2 : 2nd harmonic Fourier coefficient in dN/d ϕ with respect to the reaction plane

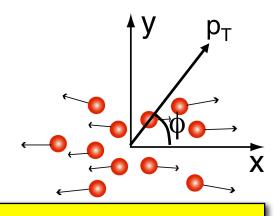


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Anisotropic/Elliptic flow



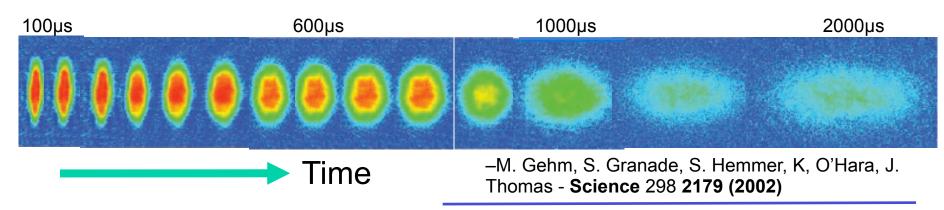




Elliptic flow observable sensitive to early evolution of system

Mechanism is self-quenching

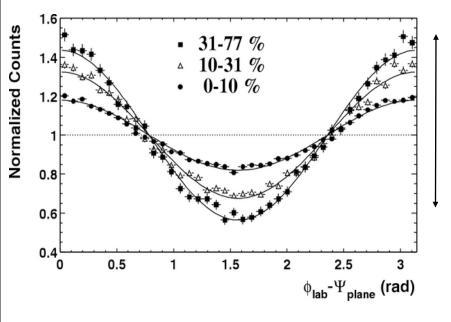
Large v₂ is an indication of early thermalization



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Elliptic flow

Distribution of particles with respect to event plane, ϕ – ψ , p_t>2 GeV; STAR PRL 90 (2003) 032301

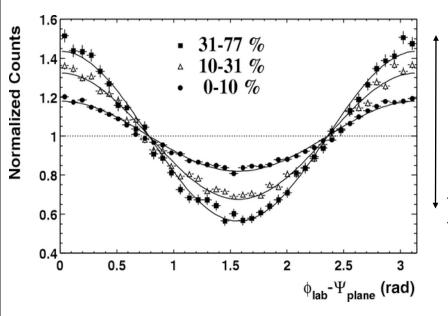


 Very strong elliptic flow → early equilibration

Factor 3:1 peak to valley

Elliptic flow

Distribution of particles with respect to event plane, ϕ - ψ , p_t>2 GeV; STAR PRL 90 (2003) 032301

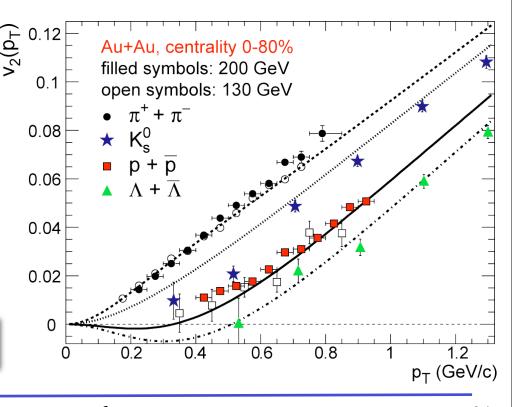


 Pure hydrodynamical models including QGP phase describe elliptic and radial flow for many species

QGP→ almost perfect fluid

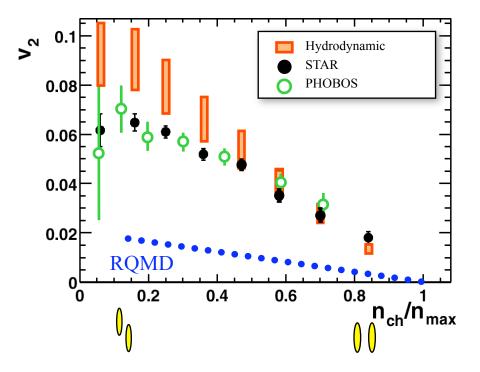
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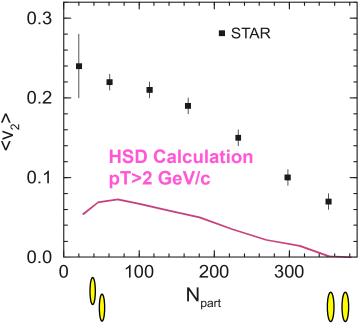
Factor 3:1 peak to valley



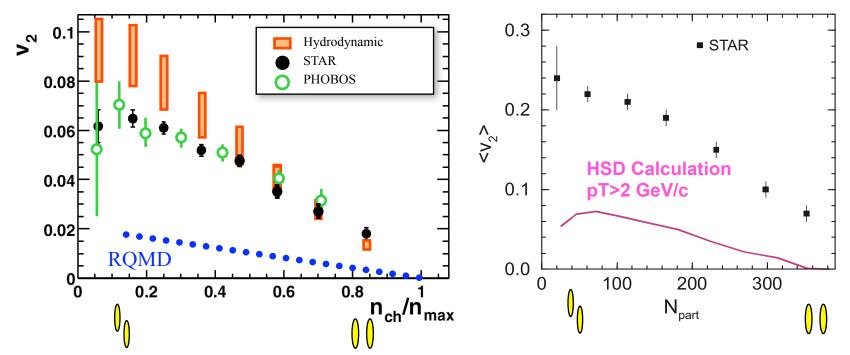
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Hadronic transport models (e.g. RQMD, HSD, ...) with hadron formation times ~1 fm/c, fail to describe data.



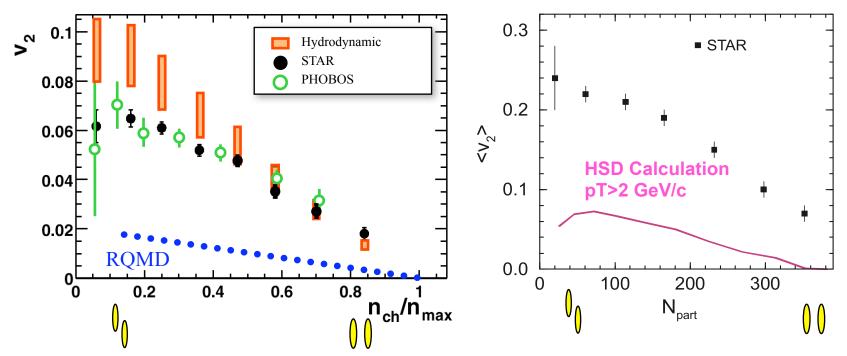


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Clearly the system is not a hadron gas. Not surprising.

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Hydrodynamical calculations:thermalization time <u>t=0.6 fm/c</u>

What interactions can lead to equilibration in < 1 fm/c?

The constituents "flow"

- Elliptic flow is additive.
- If partons are flowing the *complicated* observed flow pattern in $v_2(p_T)$ for hadrons

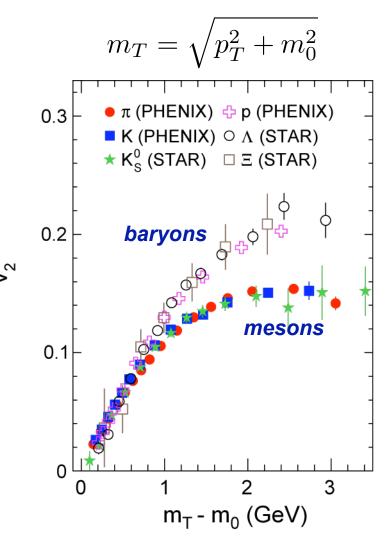
$$\frac{d^2N}{dp_T d\phi} \propto 1 + 2 v_2(p_T) \cos(2\phi)$$

should become *simple* at the quark level

$$p_T \rightarrow p_T/n$$

 $v_2 \rightarrow v_2/n$,

$$n = (2, 3)$$
 for (meson, baryon)



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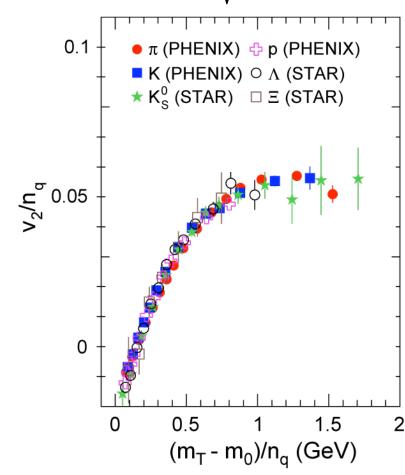
$$v_2 \rightarrow v_2 / n$$
,

n = (2, 3) for (meson, baryon)

Works for p, π , K_s^0 , Λ , Ξ ..

$$v_2^s \sim v_2^{u,d} \sim 7\%$$

$$m_T = \sqrt{p_T^2 + m_0^2}$$



Constituents of QGP are partons

Summary of what we learned so far

- Energy density in the collision region is way above that where hadrons can exist
- The initial temperature of collision region is way above that where hadrons can exist
- The medium has quark and gluon degrees of freedom in initial stages

We have created a new state of matter at RHIC - the QGP

The QGP is flowing like an almost "perfect" liquid